



redhat.

Why you shouldn't write cryptographic algorithms yourself

Experience why writing your own crypto is harder than it
seems at first.

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**Everyone tells you that you shouldn't
write your own crypto, but they don't
tell you why.**



**Instead let's see what it takes to
write software to handle a
cryptographic function like RSA***

*I chose RSA only because I had to deal with it recently, could have used any
Symmetric or asymmetric cryptographic primitive

Your Journey starts here...



The diagram illustrates the RSA encryption formula $C = M^e \bmod N$. It features three labels with arrows pointing to the corresponding parts of the equation: 'Clear text' (green) points to M , 'Public exponent' (blue) points to e , and 'Encrypted message' (orange) points to C . The modulus N is also present in the formula.

$$C = M^e \bmod N$$

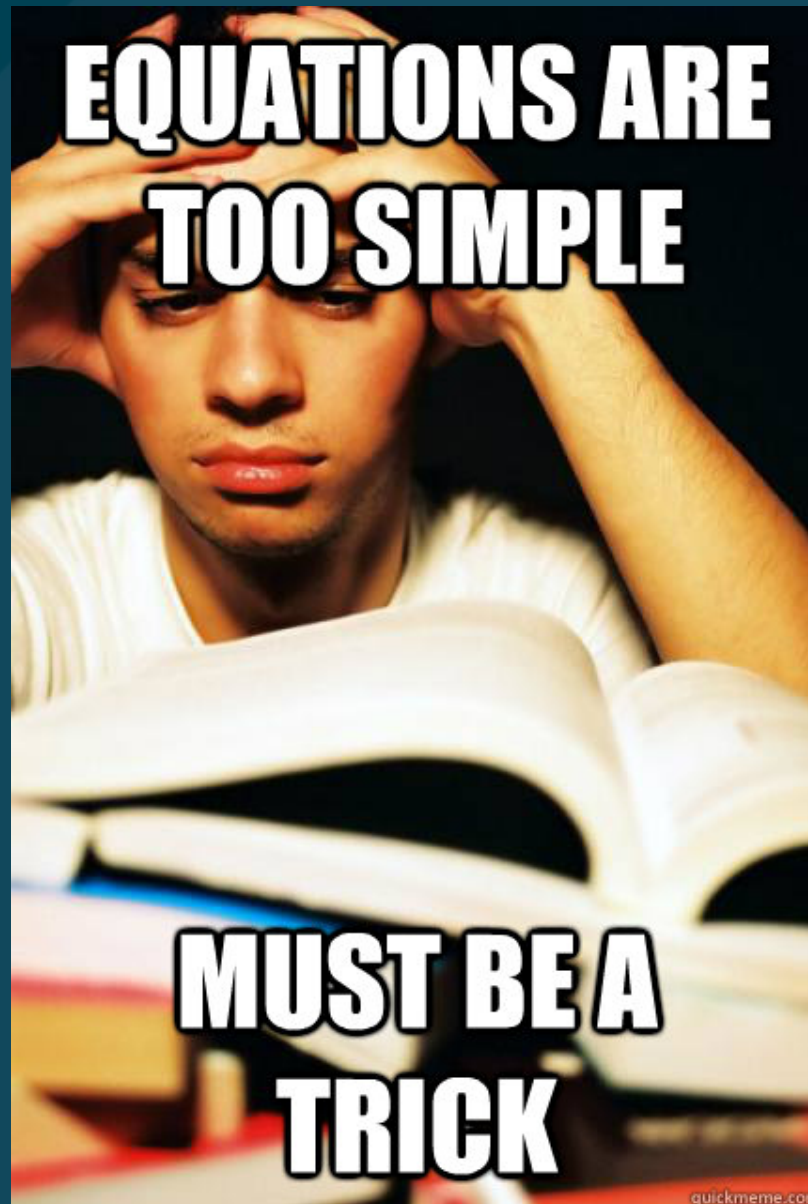
Encrypted message

Private exponent

$$M = C^d \bmod N$$

Clear text

The diagram illustrates the decryption process using the formula $M = C^d \bmod N$. Three labels with arrows point to the components of the formula: 'Encrypted message' (orange) points to 'C', 'Private exponent' (red) points to 'd', and 'Clear text' (green) points to 'M'.



**No really, no tricks!
RSA is really simple**



**Let's look at those “useless” details
the cryptographers talk about from
time to time!**

Attacks based on poor practices

Easy stuff :-)

These attacks are based on the math, not the implementation.

- Common Modulus - (Simmons)
 - Yeah, please never reuse p , q
- Low Private Exponent (d) - (Wiener)
 - Breaks cryptosystem – hey but decryption is real fast!
- Low Public Exponent (e) - (Coppersmith, Hastad, Franklin-Reiter)
 - Not a total break, but still please use $e > 2^{16} - 1$
 - Also use randomized padding
- ... for more details, search for:
 - Twenty Years of Attacks on the RSA Cryptosystem (Dan Boneh)

WE LOOKED AT THE MATH!!!



Basic tools needed to implement RSA

Usually beyond what standard languages provide

- Infinite precision math library
 - You really need to deal with **BIG** numbers, as in several thousands bits large numbers, so they won't fit in your processor registers as normal integers, or long integers or even long long integers, and you can't use floats.
- Fast, prime number generation tools to find good large primes
 - For key generation
- A good CSPRNG
 - Also for key generation and other things

RSA decryption using GMP*

Simplest code

```
/* compute root (raise to private exponent) */  
mpz_powm(message, ciphertext, key->d, key->n);
```

1

This is a bit slow ...

*GNU Multiple Precision Arithmetic Library



Faster RSA decryption

A bit faster using CRT

$$M = C^d \bmod N$$



$$\begin{aligned} dp &= d \bmod (P - 1) & dq &= d \bmod (Q - 1) \\ Mp &= C^{dp} \bmod P & Mq &= C^{dq} \bmod Q \\ \text{Find: } M &= Mp \bmod P == Mq \bmod Q \end{aligned}$$

```
/* compute root (derived from CRT) */
mpz_fdiv_r(m_mod_p, C, key->p);
mpz_powm(Mp, m_mod_p, key->a, key->p);

mpz_fdiv_r(m_mod_q, ciphertext, key->q);
mpz_powm(Mq, m_mod_q, key->b, key->q);

mpz_sub(tmp1, Mp, Mq);
mpz_mul(tmp2, tmp1, key->c);
mpz_fdiv_r(Xp, tmp2, key->p);

mpz_mul(tmp1, key->q, Xp);
mpz_add(M, tmp1, Mq);
```

x10

Attacks on implementations

Where **everyone** gets it wrong the first 42 times!

These attacks use math to defeat implementation issues.
They all need an *Oracle*, conveniently any TLS server is one.

- Timing attacks (Kocher)
 - Use blinding to defeat this (Rivest)
- Random Faults (Boneh, DeMillo, and Lipton)
 - Check signature before sending out
- Bleichenbacher's Attack on PKCS 1 (Bleichenbacher)
 - In TLS defeated by using a random session key instead of returning error

Blinding

Prevents using the server as a signing Oracle

$$M = C^d \bmod N$$



$$\begin{aligned} Cr &= C * r^e \bmod N \\ M * r &= Cr^d \bmod N \\ M &= Cr^d / r \bmod N \end{aligned}$$

```
random_func(R); /* generate random R */
mpz_invert(Ri, R, key->n); /* ..and its inverse Ri */

/* blinding */
mpz_powm(tmp1, R, key->e, key->n);
mpz_mul(tmp2, tmp1, C);
mpz_fdiv_r(Cr, tmp2, key->n);

rsa_compute_root(Mr, Cr);

/* unblinding */
mpz_mul(tmp1, Mr, Ri);
mpz_fdiv_r(M, tmp1, key->n);
```

x2

Checking

Prevents sending faulty signatures

$$M = C^d \bmod N$$

+

$$C = M^e \bmod N$$

```
/* blinding */
rsa_blind(Cr, Ri, C);

rsa_compute_root(Mr, Cr);

/* check */
mpz_powm(Cr2, Mr, key->e, key->n);
if(Cr2 != Cr) goto error;

/* unblinding */
rsa_unblind(M, Ri, Mr);
```

+2

One defense from Bleichenbacher

```
if (error) {  
    random_func(M);  
    return M;  
}
```

+2





**ERROR: YOU ARE NOT
DEPRESSED ENOUGH**

Attacks based on CPU architecture

Here is where people give up! :-)

These attacks use timing and caching issues to retrieve your keys. They all need a *LOCAL Oracle*, conveniently any TLS server on a *SHARED* host is one.

- The 9 Lives of Bleichenbacher's CAT: New Cache Attacks on TLS Implementations (Ronen, Gillham, Genkin, Shamir, Wong, Yarom)
 - Attacks the RSA implementation by timing how much time computations take
 - Attacks the RSA implementation by checking which memory area is accessed and when via CPU cache inspection and manipulation
- Funny note: OpenSSL did not raise a CVE because their threat model does not involve protecting from "local" attacks ...
 - Do you run Virtual Machines or Containers ?

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Defeating Cache/Timing attacks

Or at least we tried to ...

Luckily some of this work was already done to solve other timing issues

- GMP needs “security” functions that compute in constant time and constant space
 - `mpz_powm` → `mpn_sec_powm`
 - ...
- Change `rsa_compute_root()` to be side-channel silent
 - Remove **all input dependent** conditional operations
 - 1 function of about 10 lines → 8 functions for a total of about 100 lines
 - Obviously slower, also a lot more complicated
- Change `pkcs1 (de)padding` function to be side-channel silent
 - 1 function of about 20 lines → 2 functions for a total of about 40 lines
- All considered about 40 commits upstream

Example

```
memcpy(message, terminator + 1, message_length);  
*length = message_length;
```



```
/* fill destination buffer fully regardless of outcome. Copies the message  
 * in a memory access independent way. The destination message buffer will  
 * be clobbered past the message length. */  
shift = padded_message_length - buflen; x3 - x5  
cnd_memcpy(ok, message, padded_message + shift, buflen);  
offset -= shift;  
/* In this loop, the bits of the 'offset' variable are used as shifting  
 * conditions, starting from the least significant bit. The end result is  
 * that the buffer is shifted left exactly 'offset' bytes. */  
for (shift = 1; shift < buflen; shift <= 1, offset >= 1)  
{  
    /* 'ok' is both a least significant bit mask and a condition */  
    cnd_memcpy(offset & ok, message, message + shift, buflen - shift);  
}  
  
/* update length only if we succeeded, otherwise leave unchanged */  
*length = (msglen & (-(size_t) ok)) + (*length & ((size_t) ok - 1));
```

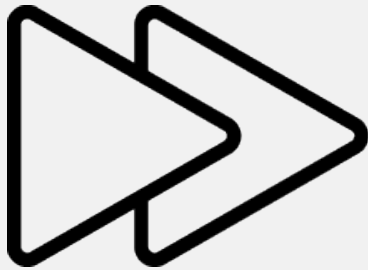
**From naive to reasonably secure
implementation**



**Two orders of magnitude more code
(... and bugs ?)**

Chose ~~Two~~ One

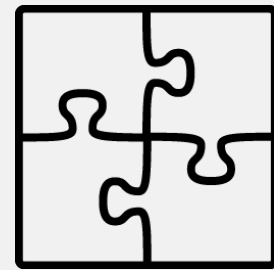
Compromises are necessary



FAST



SECURE



SIMPLE



THANK YOU



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